Gene regulatory networks reconstruction from simulated System Genetics data what we tried, what we learnt

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StatSeq meeting - Paris

Friday 29th March 2013

SaAB, MIA-T (StatSeq)

GRN reconstruction from SG data

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- Issues here: (i) formal adequate modelling framework and (ii) identification of a network that best represents the system.
- Focus in this presentation on (simulated) 'Systems Genetics' or 'Genetical Genomics' data, only looking at the level of genes.

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Dataset generation recipe

Choose simulation parameters, choose a network, generate individual genotypes and then simulate steady-state gene g expression data from:

$$\frac{\mathrm{d}\,G_g}{\mathrm{d}\,t} = Z_g^c \cdot V_g \cdot \theta_g^{syn} \cdot \prod_k \left(1 + A_{k,g} \frac{G_k^{h_{k,g}}}{G_k^{h_{k,g}} + (K_{k,g}/Z_k^t)^{h_{k,g}}} \right) - \lambda_g \cdot \theta_g^{deg} \cdot G_g$$

from SvsGenSIM, [Pinna et al. 2011] SaAB, MIA-T (StatSeq) GRN reconstruction from SG data 2013 3 / 21

Cis regulation

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$$\underbrace{\mathsf{M}_1}_{\mathsf{E}_1} \underbrace{\mathsf{M}_2}_{\mathsf{E}_2} \underbrace{\mathsf{M}_3}_{\mathsf{E}_i \in \mathbb{R}} \underbrace{\mathsf{M}_i = 0 \text{ or } 1}_{\mathsf{M}_1 = 1}$$

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Marker multifactorial effect visualisation

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- random forests (RF; has integrated bootstrap)

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Data bootstrap [Efron 1981]

- ► strategy used to get confidence on predictions and overcome noise effect.
- ▶ implementation: randomly draw (with replacement) N_{boot} replicate data-sets of identical sample size as the original data, replicate the computation (drawback 1) and store the N_{boot} models to estimate distribution of the desired statistics (e.g. edge weight).
- ► did not make use of the offered possibility to study the behaviour of any (lack of) fitness function (e.g. likelihood, MSE) from out-of-bootstrap samples (but for RF) since each replicate doesn't use ~ 37% of the original samples (drawback 2 when n is small).

Solve individual linear regression for each gene:

$$E_g = \sum_{j=1}^p \alpha_{gj} M_j + \sum_{\substack{j=1\\j \neq g}}^p \beta_{gj} E_j + \varepsilon_g$$

Since n < p, assumption that few (α, β) 's are 0 (makes GRN sparse), penalised regression methods such as the lasso or the Dantzig selector were chosen.

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lasso penalisation [Tibshirani 1996]

Both shrinks (bias) and selects variables according to:

$$\begin{split} (\hat{\alpha}, \hat{\beta})^{lasso} &= \arg\min_{\alpha, \beta} || \ E - M\alpha - E\beta \ ||_{\ell_2}^2 + \lambda \ || \ (\alpha, \beta) \ ||_{\ell_1} \\ &= \arg\min_{\alpha, \beta} || \ E - M\alpha - E\beta \ ||_{\ell_2}, \ \text{subject to} \ \ || \ (\alpha, \beta) \ ||_{\ell_1} \leq t \end{split}$$

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Dantzig selector [Candès & Tao 2007]

Slightly different constaint (related to gradient of RSS):

$$\begin{aligned} (\hat{\alpha}, \hat{\beta})^{dantzig} &= \arg\min_{\alpha, \beta} \mid\mid (\alpha, \beta) \mid\mid_{\ell_{1}} \text{ s.t. } \mid\mid (E, M)^{\top} (E - M\alpha - E\beta) \mid\mid_{\ell_{\infty}} \leq \delta \\ &= \arg\min_{\alpha, \beta} \mid\mid (E, M)^{\top} (E - M\alpha - E\beta) \mid\mid_{\ell_{\infty}}, \text{ s.t. } \mid\mid (\alpha, \beta) \mid\mid_{\ell_{1}} \leq t \end{aligned}$$

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Building weights for edges predictions

Our strategy

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- ► Estimate weights $w_{M_j \to E_g}$ by the ratio of $\alpha_{gj}^{boot,pen} \neq 0$ and $w_{E_j \to E_g}$ by $\frac{\#\{\beta_{gj}^{boot,pen} \neq 0\} + \#\{\beta_{jg}^{boot,pen} \neq 0\}}{4qN_{boot}}$: post-symetrisation of $E_g \to E_{g'}$ edges and higher confidence in $M_g \to E_{g'}$ relationships.

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- ► [Bach 2008] established that under "some conditions" (sparsity, size effect and unique λ_n), the bootstrap lasso identifies correct edges with probability 1 and selects false positives with probability < 1 when n → ∞. Our ranking should be related to edge existence !</p>

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- ► Algorithm for BN inference are of two kinds: based either on independence tests or on scores: Bayesian (BD, BDeu...) or information theoretic (AIC, BIC ...).
- ► NP hard problem (even if indegree ≤ 2 [Chickering 1996]): a simple greedy search is already very computation demanding: number of parents limited to 5.

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- Selected DAG with highest BDeu score among 3 restarts a Stochastic Greedy Search algorithm with extended local move operators (SGS3, see [Vandel et al. 2012]).
- 6. Scores are then simply the ratio of edge detection among the bootstraps.

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Other cleverer post-processings can be built but time was lacking to thoroughly assess them in the different configurations !

Results 1: AUPR for 1,000 gene networks

	AUPR with edge orientations				AUPR without edge orientations			
	Methods				Methods			
Network/configuration/data-set	Lasso	Dantzig	RF	BN	Lasso	Dantzig	RF	BN
Net4-Conf1-DS25-300SH	11.65	12.02	9.63	14.20	15.76	16.41	11.06	15.90
Net4-Conf2-DS26-900SH	15.88	15.66	17.95	18.30	21.97	21.68	20.05	20.08
Net4-Conf3-DS27-300SL	11.20	11.35	3.88	11.83	16.64	17.18	5.29	15.01
Net4-Conf4-DS28-900SL	21.49	21.78	9.64	27.28	32.46	33.30	11.31	32.95
Net4-Conf5-DS29-300DH	4.89	5.02	7.31	7.13	6.97	7.29	8.41	8.60
Net4-Conf6-DS30-900DH	9.68	10.05	13.82	20.15	13.81	14.53	15.60	22.23
Net4-Conf7-DS31-300DL	8.60	9.57	3.09	13.18	13.07	14.95	4.38	16.59
Net4-Conf8-DS32-900DL	16.20	17.43	7.39	23.24	24.20	26.71	9.12	28.76
Net5-Conf1-DS33-300SH	16.05	15.71	16.16	16.96	21.52	21.27	17.81	18.89
Net5-Conf2-DS34-900SH	22.17	21.71	23.96	30.46	31.08	30.64	26.28	32.25
Net5-Conf3-DS35-300SL	14.55	14.61	5.56	13.28	21.69	22.10	7.42	16.89
Net5-Conf4-DS36-900SL	24.57	24.70	13.53	25.56	37.38	37.85	15.86	31.37
Net5-Conf5-DS37-300DH	6.66	6.74	9.04	8.71	9.34	9.63	10.58	10.27
Net5-Conf6-DS38-900DH	12.80	12.67	21.76	23.74	17.55	17.76	23.73	25.66
Net5-Conf7-DS39-300DL	10.71	11.16	3.60	15.36	17.10	18.19	5.20	18.71
Net5-Conf8-DS40-900DL	17.42	17.92	11.04	25.57	26.33	27.75	12.86	30.71
Net6-Conf1-DS41-300SH	13.07	12.83	13.34	15.75	17.90	17.64	15.05	17.72
Net6-Conf2-DS42-900SH	17.54	17.59	23.63	24.13	24.81	24.80	25.56	26.14
Net6-Conf3-DS43-300SL	12.62	12.72	4.32	13.40	19.00	19.38	5.64	17.02
Net6-Conf4-DS44-900SL	20.72	21.07	10.67	20.14	32.06	32.72	12.69	26.12
Net6-Conf5-DS45-300DH	5.43	5.51	7.41	5.70	7.79	7.98	8.83	6.98
Net6-Conf6-DS46-900DH	8.55	8.43	15.90	12.34	11.91	11.95	17.67	14.13
Net6-Conf7-DS47-300DL	8.70	9.23	2.57	10.07	13.69	14.84	3.98	13.42
Net6-Conf8-DS48-900DL	14.68	15.33	7.82	16.11	22.86	24.41	10.06	21.36

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- ► Sample size *n*: the larger, the better !
- ► Higher gene expression heritability gives better results.
- ► Sparse chromosome genetic contents are more easily to unravel.
- BUT this is "in principle": gene expression heritability and marker density are interlocked:

	Gene expression heritability		
Chromosome density	High	Low	
Dense	00	00	
Sparse	00	<u>99</u>	

Results 3: Effect of bootstraps



Mitigated good news.

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GRN reconstruction from SG data

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Don't want to feel to depressed ? [Marbach et al 2012]'s wisdom of crowds: an infinite number of independent (better than random) inference methods is consistent !

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Post-processing also matters !



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Post-processing also matters !



But this may be the other way round on another configuration !

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Which edges are we NOT able to grab?

It's not really an issue of edge direction.

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Which edges are we NOT able to grab ?

It's not really an issue of edge direction. But what are we trying to infer: (absolute correlations between gene expressions)



Same situations for correlations between markers and gene expressions

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Image: A math a math

Which edges are we NOT able to grab?

Into details:



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Which edges are we NOT able to grab?

Into details:



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Which edges are we NOT able to grab ?

Into details:



Logically, we get $G_{21} \leftrightarrow G_{95}$ as prediction No. 12, $G_{34} \rightarrow G_{95}$ as No. 19, $G_{44} \rightarrow G_{21}$ as No. 192 (reverse is No. 214), $G_{34} \rightarrow G_{21}$ as No. 252... $G_{50} \rightarrow G_{21}$ is prediction No. 2449, $G_{50} \rightarrow G_{95}$ is No. 6559 ... and many more FP inbetween !!

Building longer/shorter paths ?

Shorter path length comparison



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Critical look on our work

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Critical look on our work

- Let's be honest, I thought methodology was almost ready for a nice package that would propose state-of-the-art efficient GRN recovery from Systems Genetics data.
- Lessons from this data set analysis: not there yet ! Was it too difficult ? Too exotic ? At least it kept us occupied full-time during summer 2012 !
- Penalised linear regressions, BN, RF ... are nice models, which actually capture some important interactions with an acceptable degree of precision but: room for improvement ??

Future work

 Still some work to be done: try data transform (no magic remedy) ? Other naive/sophisticated Machine Learning tools (neural networks, SI algorithms ...) ? Assess the impact of missing information (function, gene) in the system ? Evaluate the potential to find direct causal relationships on other data sets ?

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- Biologists might have the answer: we want to do computational biology, not (in fact we do that from time to time) pure mathematics we stick to biological problems. The more complex the biological phenomenon to account for, the more granularity in the model ? At least forward and backward (and vice versa) movement between modelling and experimental validation ! Compare model and biological reality it should represent !!

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- Many thanks for your attention !

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