Combining co-expression and co-location for gene network inference in porcine muscle development in late gestation

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General context, an interdisciplinary network

A fundamental molecular question, the regulation of gene expression An ethical and economic breeding problem, survival at birth A statistical question, modelization of gene co-expression with adding biological information



Biological context: a fundamental molecular question

Interpretation of phenotypes not explained only by genetic approach.
The same genome sequence produce a wide range of differentiated cells.
Modulation of gene expression: Epigenetic marks and chromatin regulation, cis and trans regulation → 3D nuclear topography.....

Response to physiological context: growth, health, reproduction, adaptation



Biological context: a fundamental molecular question



Hierarchical Transcription in a Multigene Complex

Biological context: an increased mortality at birth



The selection for more prolificacy and meat production has been accompanied by a substantial increase in mortality of piglets at birth

14 % of newborns died between birth and weaning

Peak of mortality in the first two days after birth \iff maturity

Figure 1. Evolution of average number of piglets per litter in France from 1975 to 2015. The data used to build this graph were collected and treated by the GTTT (Technical Management of Sow Herds) of the French Porc and Pig Institut (IFIP).

Specific mechanisms during late gestation in pigs

Maturity = plain development allowing survival at birth







Wilson et al., 1998 ; Biensen et al., 1998 ; Leenhouwers et al., 2002 ; Canario, 2006 ; Thèse de Valentin Voillet, 2016

Specific mechanisms during late gestation in pigs – muscle tissue



ANR project PORCINET (2010)

A dramatic switch of gene expression occurred in late gestation



PCA without variables selection



5,167 genes differential between 90 and 110 dg in the fetal muscle (Bonferroni 1%)

With 1,131 DEGs for age x genotype (maturity) found in Voillet et al. (2014)

IGF2, a gene of fundamental importance in pig muscle development



IGF2 (pat), insulin-like growth factor 2

Pig → QTL for adiposity muscle mass
Human → fetal growth and intrauterine growth restriction

Co-expression = co-regulation? = nuclear co-localization?



1. Network inference with GGM

2. Coming back to our problem: gene expression and FISH experiments

Hypothetizing that co-expression is related to co-location:

 have an automated process to automatically find relevant pairs of genes for which co-location can be tested (because FISH experiments are time consumming and targeted experiments)

improve network inference using co-location information

1. Network inference with GGM

Framework



here: micro-array experiment, n = 61 (gestational age: 90 days) and p = 13,855 uniquely annotated genes

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What we want to obtain: a network with

- nodes: genes;
- edges: large and direct co-expression between two genes (track transcription regulations)

Butte and Kohane (1999, 2000)

First (naive) approach: calculate correlations between expressions for all pairs of genes, threshold the smallest ones and build the network.



"Correlations"





Thresholding

Graph









Networks are built using partial correlations, i.e., correlations between gene expressions knowing the expression of all the other genes (residual correlations).

Gaussian Graphical Model (GGM)

 $(X_i)_{i=1,...,n}$ are i.i.d. Gaussian random variables $\mathcal{N}(0, \Sigma)$ (gene expression); then

 $j \longleftrightarrow j' (\text{genes } j \text{ and } j' \text{ are linked}) \Leftrightarrow \mathbb{C}\mathrm{or}\left(X^{j}, X^{j'} | (X^{k})_{k \neq j, j'}\right) \neq 0$

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 $\mathbb{C}\mathrm{or}\left(X^{j}, X^{j'} | (X^{k})_{k \neq j, j'}\right) \simeq \left(\Sigma^{-1}\right)_{j, j'} \Rightarrow \text{find the partial}$ correlations by means of $(\widehat{\Sigma}^{n})^{-1}$.

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Problem: Σ is a *p*-dimensional matrix (with *p* large) and *n* is small compared to $p \Rightarrow (\widehat{\Sigma}^n)^{-1}$ is a poor estimate of Σ^{-1} !

Sparse approaches

Relation between partial correlation and LM: if $S = \Sigma^{-1}$ and writing

$$X^{j} = \beta_{j}^{\top} X^{-j} + \epsilon$$

we have: $\beta_{jj'} = \frac{S_{jj'}}{S_{jj}}$. So edges (non zero partial correlations) also correspond to coefficients different to zero in the *p* regression models above (for j = 1, ..., p).

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To ensure sparsity of β_j : Meinshausen and Bühlmann (2006)

$$\operatorname{argmin}_{\beta_j} \sum_{i=1}^n \left(x_i^j - \beta_j^\top x_i^{-j} \right)^2 + \lambda \|\beta_j\|_{\ell_1}$$

Including prior knowledge in this model

Suppose that we have some clues that:

- for some pairs (j, j'), an edge is likely to occur between j and j'
- for some pairs (j, j'), it is likely that there is no edge between j and j'

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then, we want to drive $\beta_{jj'}$

- toward ±a with a some positive value (the sign is that of the correlation Cor(X^j, X^{j'}))
- toward 0

Including another penalty in the model

$$\operatorname{argmin}_{\beta_{j}} \sum_{i=1}^{n} \left(x_{i}^{j} - \beta_{j}^{\top} x_{i}^{-j} \right)^{2} + \lambda \|\beta_{j}\|_{\ell_{1}} + \underbrace{\mu \left(\sum_{j' \text{ of type } 1} (\beta_{jj'} \pm a)^{2} + \sum_{j' \text{ of type } 2} (\beta_{jj'})^{2} \right)}_{j' \text{ of type } 1}$$

smooth penalty for co-localized (or not) pairs

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smooth penalty for co-localized (or not) pairs

In practice:

- *a* = 1 (after scaling of gene expressions)
- λ chosen with stability selection based on bootstrap for a fixed μ
- μ chosen as the minimum value recovering exactly prior knowledge

2. Coming back to our problem: gene expression and FISH experiments restricted to a list of genes likely involved in foetal development (1,131 DEGs between 90 and 110 days of gestation as found in Voillet et al. (2014)) restricted to a list of genes likely involved in foetal development (1,131 DEGs between 90 and 110 days of gestation as found in Voillet et al. (2014))

 started from an even more restricted list including genes of interest (*IGF2*, *DLK1* and *MEG3*) and the genes highly correlated to these genes (p = 359 genes at the end)

Iterative process: from co-location to network and conversely



- 1. Node importance
- 2. Clustering of nodes (and comparison of clustering with NMI)
- 3. GO analysis

- degree (number of edges afferent to a given node)
- betweenness centrality measure



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Find clusters by modularity optimization

The modularity Newman and Girvan (2004) of the partition (C_1, \ldots, C_K) is equal to:

$$\mathcal{Q}(\mathcal{C}_1,\ldots,\mathcal{C}_K) = rac{1}{2m}\sum_{k=1}^K\sum_{x_i,x_j\in\mathcal{C}_k}\left(W_{ij}-P_{ij}\right)$$

with P_{ij} : weight of a "null model" (graph with the same degree distribution but no preferential attachment):

$$\mathsf{P}_{ij} = \frac{d_i d_j}{2m}$$

with $d_i = \frac{1}{2} \sum_{j \neq i} W_{ij}$.

Interpretation of the modularity

A good clustering should maximize the modularity:

- $Q \nearrow$ when (x_i, x_j) are in the same cluster and $W_{ij} \gg P_{ij}$
- $Q \searrow$ when (x_i, x_j) are in two different clusters and $W_{ij} \gg P_{ij}$ (m = 20)

$$d_i = 15$$
 $P_{ij} = 7.5$ $d_j = 20$
 $W_{ij} = 5 \Rightarrow W_{ij} - P_{ij} = -2.5$

i and *j* in the same cluster decreases the modularity

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$$d_i = 1$$
 $P_{ij} = 0.05$ $d_j = 2$
 $W_{ij} = 5 \Rightarrow W_{ij} - P_{ij} = 4.95$

i and *j* in the same cluster increases the modularity

Interpretation of the modularity

A good clustering should maximize the modularity:

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- $Q \searrow$ when (x_i, x_j) are in two different clusters and $W_{ij} \gg P_{ij}$
- Modularity
 - helps separate hubs
 - is not an increasing function of the number of clusters: useful to choose the relevant number of clusters

Approximate optimization with the Louvain algorithm Blondel et al. (2008) (among others)

359 DEGs were selected for being highly correlated with *IGF2*, *DLK1* and *MEG3* ($R^2 \ge 0.84$)

- Network 0 to 3 with 359 nodes
- → Network 0 without *a priori*, 2,279 edges (density: 3.55%)





Marti-Marimon et al., 2018.

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- → Network 1 with triple co-localization of *IGF2*, *DLK1* and *MEG3*, 2,250 edges (density 3.50%)



IGF2 RPL32

IGF2 and *RPL32* were associated in 20% of the analysed nuclei (threshold 10%)

Marti-Marimon et al., 2018.

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- → Network 0 to 3 with 359 nodes
- → Network 0 without *a priori*, 2,279 edges and density 3.55%
- → Network 1 with co-localization of *IGF2*, *DLK1* and *MEG3*, 2,250 edges and density 3.50%
- → Network 2 with test of *MEST* and *DCN* associations, 2,091 edges and density 3.25%



Marti-Marimon et al., 2018.

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→ Network 3 with test co-localization with MYH3 (ntw 0 and 1)



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→ Network 3 with test co-localization with *MYH3* (ntw 0 and 1)

MYH3 = Embryonic myosin, excellent biomarker of muscle maturity (Voillet et al., 2018) No functional link known with IGF2!



359 DEGs were selected for being highly correlated with *IGF2*, *DLK1* and *MEG3* ($R^2 \ge 0.84$)

→ Network 3 with test co-localization with MYH3 (ntw 0 and 1), 2,091 edges and density 3.25%



Network mining (network structure with key genes)

The **degree** of a node is the number of edges afferent to this gene. High degree genes are connected to many other genes (hub).

The **betweenness** of the node is the number of shortest paths between pairs of genes in the network that pass through that gene. High-betweenness genes are central and more likely to disconnect the network if removed.

Network mining (network structure with key genes)

	Ne	Network 0 Network 1 Network 2		Ne	etwork 3	Comparison between Network 0 and Network 3 (% of variation)				
gene symbol	degree	betweeness	degree	betweeness	degree	betweeness	degree	betweeness	Degree	betweeness
ADIPOR2	15	646,65	14	487,32	15	628,78	14	660,97	-7	2
AKR7A2	19	492,63	17	436,71	15	474,10	14	291,90	-26	-41
CD81	17	551,17	18	616,7	15	478,76	17	600,58	0	9
CRAT	19	716,24	15	518,26	16	738,30	14	573,58	-26	-20
DCN	16	438,86	18	560,83	9	288,82	6	357,74	-63	-18 🎽
DLK1	10	103,52	6	81,7	5	74,22	5	24,13	-50	-77 🎽
DPP4	15	568,91	16	672,01	15	674,94	15	597,87	0	5
EGFR	16	624,92	12	375,87	12	385,35	11	354,78	-31	-43
GHITM	16	578,58	17	588,76	16	592,35	14	496,63	-13	-14
GLUD1	13	575,69	13	553,28	12	574,48	12	586,27	-8	2
IGF2	10	118,26	11	231,09	8	260,58	7	622,44	-30	426 🖊
LPAR4	14	464,31	17	644,76	18	812,81	16	798,82	14	72
MEG3	13	282,32	5	55,75	6	120,18	5	24,13	-62	-91 🔰
MESP1	12	228,49	14	320,34	14	483,27	14	775,31	17	239
MEST	13	148,2	12	121,44	10	345,69	7	385,27	-46	160 🔰
MRPS28	16	743	15	743,29	16	953,42	15	796,14	-6	7
МҮНЗ	14	610,73	14	656,6	11	455,62	4	0,00	-71	-100 🔰
NMNAT3	17	562,63	18	664,84	16	473,55	17	573,15	0	2
RAVER1	16	613,84	16	665,73	16	696,35	16	745,66	0	21
RPL32	18	717,96	15	557,65	7	149,80	5	243,11	-72	-66 🎽
SELO	18	692,52	14	438,35	14	459,46	15	587,32	-17	-15
SYDE1	15	436,75	17	530,29	14	459,66	18	745,52	20	71
TFRC	15	595,1	15	534,83	13	437,38	17	846,81	13	42
TYRO3	20	785,95	18	659,9	16	603,94	17	700,03	-15	-11
YWHAB	20	670,22	17	470,35	17	538,41	17	547,17	-15	-18

Marti-Marimon et al., 2018.

Network clustering

To analyse the evolution of the network structure from Network 0 to Network 3, clustering of the genes was performed on each network.

Normalized mutual information (NMI) measure the similarity between two clusterings. The value is comprised between 0 and 1 and is equal to 1 when the two clusterings are identical.

→ clusterings become more consistent when introducing new biological information in each network inference iteration

	Network 0	Network 1	Network 2	Network 3
Network 0	1	0.3893	0.3381	0.3244
Network 1	0.3893	1	0.4007	0.3923
Network 2	0.3381	0.4007	1	0.4152
Network 3	0.3244	0.3923	0.4152	1

Network clustering: Networks 0 and 3 were analysed in depth to search for any correspondence between clusters

Pairwise contingency tables between clusterings. Percentage of genes for each cluster in Network 0 found in each cluster of Network 3. In bold and red, the most resembling values between clusters.

		Clusters in Network 3					
		1	2	3	4	5	6
	1	64,10	7,69	7,69	2,56	7,69	10,26
	2	8,77	68,42	0,00	1,75	19,30	1,75
	3	14,89	0,00	65,96	19,15	0,00	0,00
Clusters in	4	3,92	1,96	11,76	82,35	0,00	0,00
Notwork 0	5	34,09	6,82	4,55	11,36	43,18	0,00
Network U	6	3,57	17,86	14,29	32,14	0,00	32,14
	7	11,11	38,89	0,00	11,11	38,89	0,00
	8	0,00	48,72	33,33	10,26	5,13	2,56
	9	5,56	11,11	16,67	27,78	38,89	0,00

Functional enrichment analysis: Gene Ontology Biological Process

Functional enrichment analysis based on Gene Ontology was performed using the web tool Webgestalt (WEB-based GEne SeT AnaLysis Toolkit)

	Network 0 - Cluster 1	Network 3 - Cluster 1	
GOBP Terms	FDR	FDR	Target
Extracellular structure	5,76E-05	1,14E-08	DCN
Cellular response to organonitrogen compound	6,80E-04	1,16E-02	IGF2
Reponse to transformaing growth factor beta	2,35E-03	1,24E-01	
Multicellular organism metabolic process	2,35E-03	3,05E-03	
Skin development	3,18E-03	1,44E-01	
Neuron migration	2,82E-02	4,37E-01	
Regulation of neuron projection development	3,07E-02	4,93E-01	
Mesoderm development		1,24E-01	MEST
Muscle organ development		8,35E-01	МҮНЗ
Notch signaling pathway		5,56E-01	DLK1
Collagen fibril organization	1,10E-04	1,02E-05	
	Network 0 - Cluster 8	Network 3 - Cluster 2	
GOBP Terms	FDR	FDR	
Generation of precursor metabolites and energy	1,64E-02	1,32E-07	
Oxidation-reduction process	7,25E-03	5,63E-09	
Energy derivation by oxidation of organic compounds	8,17E-03	1,88E-06	
Cellular respiration	8,17E-03	2,65E-07	

Functional enrichment analysis: reconstructed network of genes in cluster 1 of Network 3 with Ingenuity Pathway Analysis (IPA)

IPA proposed to connecting 49 (82%) out of 60 genes in a network. *MYOD1* and *CTNNB1* were identified by upstream regulator analysis as potential transcriptional factors for a group of genes including *IGF2* and *MYH3*.



"Cell Morphology", 14 genes, *p*-value = 1.75e-08 "Quantity of cells", 31 genes, *p*-value = 2.48e-09 "Morphology of connective tissue cells", 8 genes, *p*-value = 1.27e-04

"Formation of muscle", 10 genes, *p*-value = 2.98e-05, involved IGF2 and MYH3 together with CTNNB1 and MYOD1.

Marti-Marimon et al., 2018. Villa-Vialaneix et al., 2013

Conclusions

- 82% of edges in Network 0 were conserved in Network 3
- The most important genes in Network 0 were among those showing the highest values of betweenness and degree in Network 3.
- → Not major disturbances in the network structure
- In the local analysis, the NMI value revealed that the clusters resembled one another more with each new network inferred.
- Four out of six clusters in the final network conserved more than 62% of genes in the corresponding clusters of Network 0.
- IGF2-MEST, (DLK1/MEG3)-MEST, (DLK1/MEG3)-DCN, that were observed to be connected in coexpression networks in other studies.
- *DLK1, MEG3, RPL32, MEST, DCN* and *MYH3* were less connected with the rest of the other genes in Network 3 but not *IGF2*.
- No previous association between IGF2 and MYH3, even though the two genes are known to be involved in muscle development → overexpression and accumulation of β-catenin in the nuclei of differentiating murine myoblasts results in higher MyoD activation and Myhc induction (Ramazzotti et al, 2016)

Conclusions - Perspectives

- What is published and what is not...
- Intermediate modelling is retained as valuable information on robust or non-robust interactions → currently, new interactions are being tested by FISH 3D
- Dramatic change in gene expression at the end of gestation → Search of interaction whole genome (Maria Marti-Marimon thesis)





Interaction depletion

Interaction enrichment

Whole genome interaction Maps 3D Chromosome conformation capture Hi-C in progress

Thank you for your attention!

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