

GMDPtoolbox: a Matlab library for solving Graph-based Markov Decision Processes

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System management in ecology and agriculture

Management is complex because several entities in interaction must be managed together with a long term objective with uncertain environment.



Integrated management:

- variety choice,
- cultural practices,
- soil management,
- ...



Finding an optimal (or at least a good) policy to govern these large systems is still a challenge in practice.

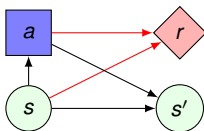
MDP

Markov Decision Processes (MDP) [Puterman 94, Sigaud *et al.* 10] provide a classical framework for modelling and solving problems of sequential decision under uncertainty.

A discrete-time stationary MDP is defined by a 4-tuple $\langle S, A, p, r \rangle$:

- S is the state space,
- A is the action space
- $p(s'|s, a)$ is the transition probability function
- $r(s, a)$ is the reward function

For a given policy δ , defines a stationary *Markov chain* over S , with transitions $p_\delta(s'|s) = p(s'|s, \delta(s))$.



MDP - Policy design

- A **policy** is defined as a function $\delta : S \rightarrow A$.

Let $v_\delta(s)$ is the value of the policy δ .

For the infinite-horizon discounted reward criterion:

$$v_\delta(s) = E \left[\sum_{t=0}^{+\infty} \gamma^t r(s^t, \delta(s^t)) \mid s^0 = s \right], \forall s \in S.$$

- Policies that maximizes v_δ can be computed in polynomial time in $|S|$ and $|A|$ using Dynamic Programming (Policy Iteration, Value Iteration...).

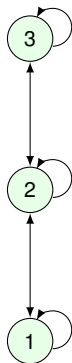
To address larger problems, several frameworks **Factored MDP** (FMDP) have been proposed for factored state or/and action spaces and policies [Guestrin *et al.* 01, Kim *et al.* 02]

GMDP

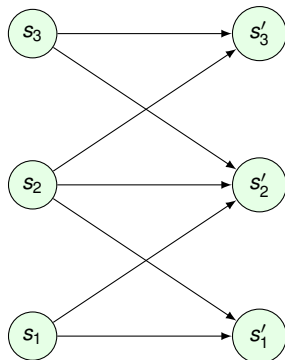
Graph-based MDP (GMDP) framework [Sabbadin *et al.* 12]

→ states, actions spaces factorisation (sites in interaction).

For a given policy, the dynamic model is a Dynamic Bayesian Network.



Neighborhood relationship



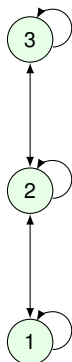
Corresponding DBN

GMDP

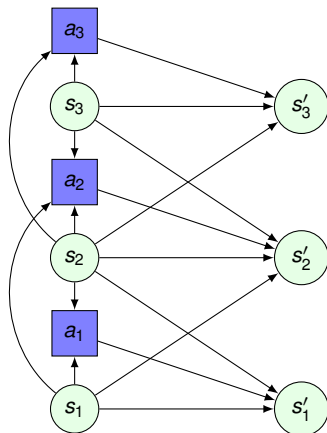
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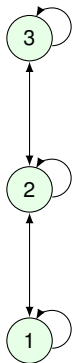
Corresponding DBN

GMDP

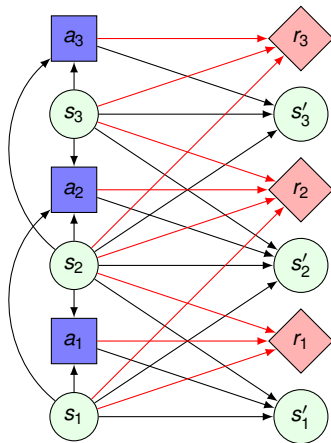
Graph-based MDP (GMDP) framework [Sabbadin *et al.* 12]

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Neighborhood relationship



Corresponding DBN

GMDP - Policy finding

A discrete-time GMDP is defined by a 5-tuple $\langle S, A, N, p, r \rangle$:

- $S = S_1 \times \dots \times S_n$
- $A = A_1 \times \dots \times A_n$
- $N = \{N_i, \forall i = 1, \dots, n\}$ with $N_i \subset \{1, \dots, n\}$
- $p = \{p_i(s'_i | s_{N_i}, a_i) \forall i = 1, \dots, n\} \rightarrow p(s' | s, a) = \prod_{i=1}^n p_i(s'_i | s_{N_i}, a_i)$
- $r = \{r_i(s_{N_i}, a_i) \forall i = 1, \dots, n\} \rightarrow r(s, a) = \sum_{i=1}^n r_i(s_{N_i}, a_i)$

Only *local policies* are considered: $\delta = (\delta_1, \dots, \delta_n)$ where $\delta_i : S_{N_i} \rightarrow A_i$

Two algorithms, providing local policies by approximate resolution of a GMDP, have been defined by [Sabbadin *et al* 12].

- **MF-API** : Mean Field Approximate Policy Iteration
Exploits the structure of the neighborhood relations of the GMDP and computes a *Mean-Field approximation* of the value function of a policy.
- **ALP** : Approximate Linear Programming
Derived from the general class of ALP algorithms, for large size MDP.

They usually find empirically good local policies.

GMDPtoolbox - An help to apprehend the framework and support studies

GMDP generation

gmdp_example_epidemi

gmdp_example_grid

gmdp_example_rand

GMDP resolution

gmdp_linear_programming

gmdp_policy_iteration_MF

gmdp_globalize

Policy description

gmdp_sec_policy

gmdp_sec_policy_tab

gmdp_sec_policy_graph

gmdp_analyze_policy

gmdp_analyze_policy_neighbor

Policy evaluation

Mean-Flat based evaluation

gmdp_eval_policy_MF

Simulation based evaluation

gmdp_simulate_policy

gmdp_eval_policy_value

gmdp_eval_policy_value_site
_contribution

gmdp_eval_policy_state_time

Evaluation of global value

gmdp_eval_policy_global_value

gmdp_eval_policy_global_value
_state

1. Describe the problem

- ▶ 3 functions available to define simple problems

2. Find a good policy

- ▶ 2 functions for MF-API and ALP
- ▶ 1 function to translate small problem in MDP format for MDPtoolbox¹ [Chadès *et al.* 14]

3. Interpret the policy

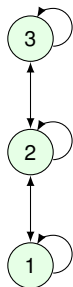
- ▶ 5 functions to apprehend and visualize policies

4. Analyse policies

- ▶ 3 functions to evaluate the value function
- ▶ 4 functions to simulate policies

¹MDP toolbox: <http://inra.fr/mia/T/MDPtoolbox>

Quick start - Epidemics management toy example



- 3 crop fields can be in two states: uninfected (1 ✓) or infected (2 ✗).
- Each field is susceptible to contamination by a pathogen.
- Two actions for a field: a normal (1 ✗) or adapted (2 ⚡) cultural mode.
- When a field is contaminated, the yield decreases.
- The problem is to optimize a long-term policy in terms of expected yield.

Quick start - Computing a policy

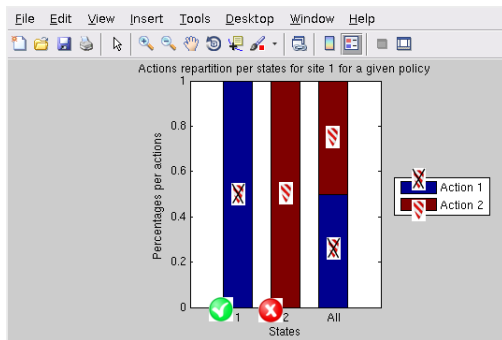
1. Describe the problem

```
>> GMDP = gmdp_example_epidemie ();
```

2. Find a good policy

```
>> policyloc = gmdp_linear_programming(GMDP, discount);
```

```
>> actions_repartition_state_site = gmdp_analyze_policy_neighbor(GMDP, policyloc);
```



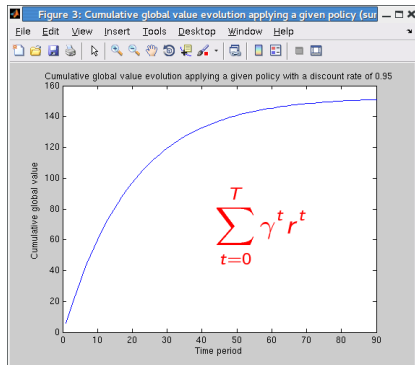
Decision rule

IF field is infected THEN apply an adapted cultural mode
ELSE apply a normal cultural mode

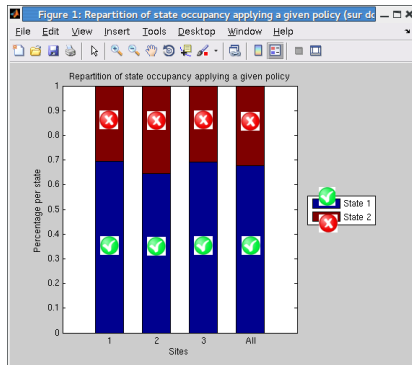
Quick start - Evaluating a policy

3 Simulate policy application

```
>> [sim_state , sim_reward] = gmdp_simulate_policy(GMDP, policyloc);  
>> value_evolution1 = gmdp_eval_policy_value(discount , sim_reward);  
>> state_time = gmdp_eval_policy_state_time(GMDP, sim_state);
```



Cumulative discounted reward



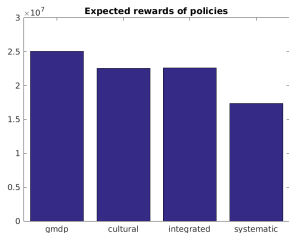
Time spent in the different site states

Evaluate pest management

- Each site is non contaminated about 65% of the time.
- This could be compared with other policies.

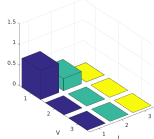
Management of phoma pest on canola crop

A grid of 100 fields, for each field 11 states, $8(2^3)$ actions, 5 neighbors.
Find a good strategy and simulate 4 policies from a given initial state.

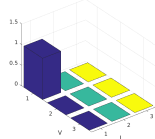


Expected cumulative rewards

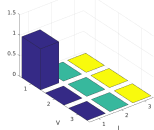
gmdp policy
Mean repartition of wheat state occupancy
on all sites, simulating gmdp policy



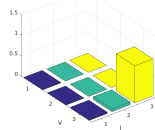
cultural policy
Mean repartition of wheat state occupancy
on all sites, simulating cultural policy



integrated policy
Mean repartition of wheat state occupancy
on all sites, simulating integrated policy



systematic policy
Mean repartition of wheat state occupancy
on all sites, simulating systematic policy



Mean state repartition in wheat state

Results

- Put on the spotlight a new interesting strategy.
- Put in evidence contrasted long term effect of policies.

Conclusion

GMDPtoolbox : A free library²that provides:

- a framework to set the problem,
- algorithms to find a good policy,
- tools to explore and analyze policies,

Perspectives

- A new version soon released providing more adapted analysis functions, and GNU Octave compatibility.
- An other solving algorithm [Cheng *et al.* 13] based on approximate Value Iteration which approximate the value function with a Belief Propagation algorithm.

Application

- GMDP framework yet used for: plant disease management [Peyrard *et al.* 07], human disease management [Choisy *et al.* 07], forest management [Forsell *et al.* 11] and invasive pest control [Nicol *et al.* 15].
- With current environment evolution (biodiversity decrease, climate change...), GMDPtoolbox could help adapting management in agriculture, epidemics control or ecology.

²GMDPtoolbox: <http://inra.fr/mia/T/GMDPtoolbox>



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