

General Linear Models Procedure

Class Level Information

Class	Levels	Values
TESTEUR	2	1 2
ORIGINE	3	1 2 3

Number of observations in data set = 12

General Linear Models Procedure

Dependent Variable : HUILE

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	5	47,18144167	9,43628833	6,18	0,0233
Error	6	9,16665000	1,52777500		
Corrected Total	11	56,34809167			

R-Square	C.V.	Root MSE	HUILE Mean
0,837321	2,671010	1,236032	46,27583

$$R^2 = \frac{SCE_{M_2} - SCE_{M_3}}{SCE_{M_0}}$$

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	I-I	$SCE_{M_0} - SCE_{M_3}$		$\frac{(SCE_{M_0} - SCE_{M_3}) / I-I}{SCE_{M_3} / N-IJ}$	
Error	N-IJ	SCE_{M_3}			
Corrected Total	N-1	SCE_{M_0}			

Tableau "Facteurs"

Dependent Variable : HUILE

Source	DF	Type I SS	Mean Square	F Value	Pr > F
TESTEUR	1	9,48740833	9,48740833	6,21	0,0470
ORIGINE	2	33,74581667	16,87290833	11,04	0,0097
TESTEUR*ORIGINE	2	3,94821667	1,97410833	1,29	0,3415

Dependent Variable : HUILE

Source	DF	Type III SS	Mean Square	F Value	Pr > F
TESTEUR	1	9,48740833	9,48740833	6,21	0,0470
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TESTEUR*ORIGINE	2	3,94821667	1,97410833	1,29	0,3415

TESTEUR	I-1	$SCE_{M_0} - SCE_{M_1}$		$\frac{(SCE_{M_0} - SCE_{M_1}) / I-1}{SCE_{M_3} / N-IJ}$
ORIGINE	J-1	$SCE_{M_1} - SCE_{M_2}$		$\frac{(SCE_{M_1} - SCE_{M_2}) / J-1}{SCE_{M_3} / N-IJ}$
TESTEUR*ORIGINE (I-1)(J-1)		$SCE_{M_2} - SCE_{M_3}$		$\frac{(SCE_{M_2} - SCE_{M_3}) / (I-1)(J-1)}{SCE_{M_3} / N-IJ}$

```

1 143,54      data trv ;
1 1 45,30      infile 'tourm' ;
1 2 44,25      input testeur origine huile ;
1 2 42,55      run ;
1 3 47,28      proc glm ;
1 3 49,40      class testeur origine ;
2 1 47,21      model huile = origine testeur testeur*origine ;
2 1 47,73      run ;
2 2 44,34
2 2 46,49
2 3 47,75
2 3 49,47

```

$$M_3 \text{ (testeur + origine + interaction testeur x origine)}$$

$$\mu_{ij} = \mu + \alpha_i + \beta_j + \gamma_{ij}$$

$$M_2 \text{ (testeur + origine)}$$

$$\mu_{ij} = \mu + \alpha_i + \beta_j$$

$$M_1 \text{ (origine)}$$

$$\mu_{ij} = \mu + \beta_j$$

$$M_0$$

$$\mu_{ij} = \mu$$

Sortie SAS

General Linear Models Procedure

Class Level Information

Class	Levels	Values
Testeur	2	1 2
Origine	3	1 2 3

Number of observations in data set = 12

General Linear Models Procedure

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Error	6	9,16665000	1,52777500		
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	R-Square	C.V.	Root MSE	HUILE Mean	
	0,837321	2,671010	1,236032	46,27583	

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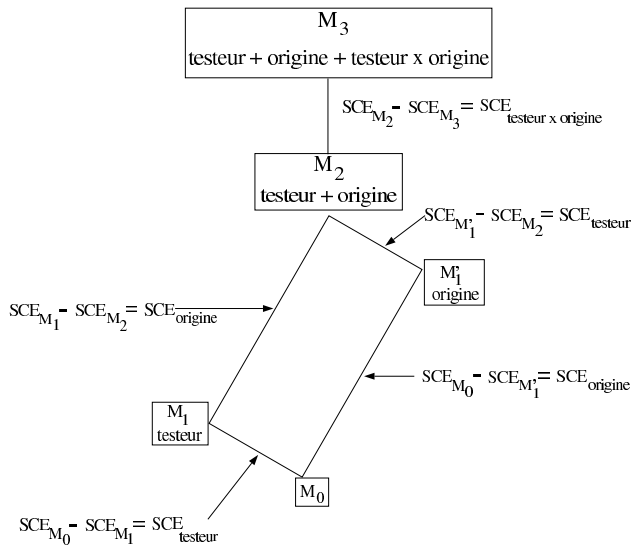
Dependent Variable : HUILE

Source	DF	Type I SS	Mean Square	F Value	Pr > F
ORIGINE	2	33,74581667	16,87290833	11,04	0,0097
TESTEUR	1	9,48740833	9,48740833	6,21	0,0470
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Dependent Variable : HUILE

Source	DF	Type III SS	Mean Square	F Value	Pr > F
ORIGINE	2	33,74581667	16,87290833	11,04	0,0097
TESTEUR	1	9,48740833	9,48740833	6,21	0,0470
TESTEUR*ORIGINE	2	3,94821667	1,97410833	1,29	0,3415

ORIGINE	J-1	$SCE_{M_0} - SCE_{M_1}$	$\frac{(SCE_{M_0} - SCE_{M_1})}{SCE_{M_3} / N-U} / J-1$
TESTEUR	I-1	$SCE_{M_1} - SCE_{M_2}$	$\frac{(SCE_{M_1} - SCE_{M_2})}{SCE_{M_3} / N-U} / I-1$
TESTEUR*ORIGINE (I-1)(J-1)	$(I-1)(J-1)$	$SCE_{M_2} - SCE_{M_3}$	$\frac{(SCE_{M_2} - SCE_{M_3})}{SCE_{M_3} / N-U} / (I-1)(J-1)$



SCE type I = SCE type III

Une unique décomposition de la somme des carrés des écarts totale :

$$SCE_{totale} = SCE_{testeur} + SCE_{origine} + SCE_{testeur \times origine} + SCE_{résiduelle}$$

Plan orthogonal : que teste-t-on avec les tests F ?

Plan orthogonal \Leftrightarrow SCE type I = SCE type III

	F	H_0
origine	$\left\{ \begin{array}{l} \frac{(SCE_{M_0} - SCE_{M_1}) / J - 1}{SCE_{M_3} / N - IJ} \\ = \\ \frac{(SCE_{M_1} - SCE_{M_2}) / J - 1}{SCE_{M_3} / N - IJ} \end{array} \right.$	$\left\{ \begin{array}{l} \forall j \\ \beta_j + \frac{\sum_i \gamma_{ij}}{I} = 0 \end{array} \right.$
testeur	$\left\{ \begin{array}{l} \frac{(SCE_{M_0} - SCE_{M_1}) / I - 1}{SCE_{M_3} / N - IJ} \\ = \\ \frac{(SCE_{M_1} - SCE_{M_2}) / I - 1}{SCE_{M_3} / N - IJ} \end{array} \right.$	$\left\{ \begin{array}{l} \forall i \\ \alpha_i + \frac{\sum_j \gamma_{ij}}{J} = 0 \end{array} \right.$
testeur x origine	$\frac{(SCE_{M_2} - SCE_{M_3}) / IJ - 1}{SCE_{M_3} / N - IJ}$	$\left\{ \begin{array}{l} \forall (i, j) \\ \gamma_{ij} = 0 \end{array} \right.$

cas non orthogonal

(pas de case vide)

3 variétés de carottes cultivées dans 2 sols

Y : nombre de jours avant germination

Données expérimentales

Y_{ijr}	Variété 1	Variété 2	Variété 3
Sol 1	6 10 11	13 15	14 22
Sol 2	12 19 15 18	31	18 9 12

ex : dispositif déséquilibré

Facteur A = sol

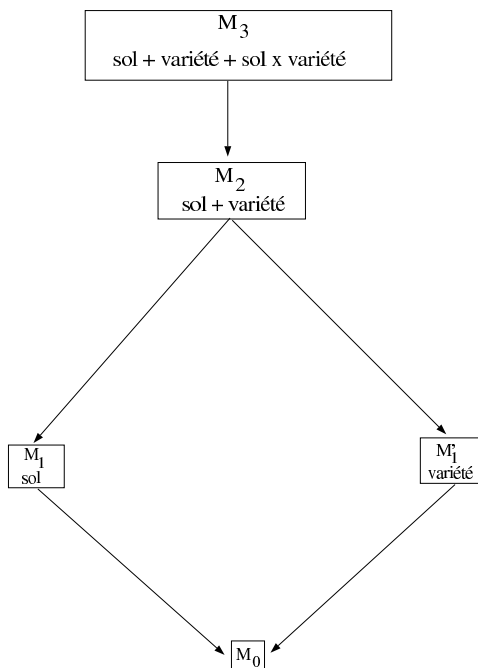
I = 2 niveaux

Facteur B = variété

J = 3 niveaux

Fichier des données

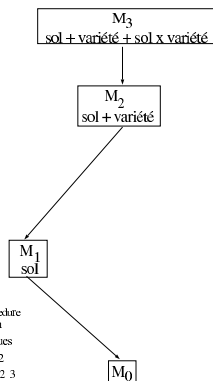
1 1 16
1 1 10
1 1 11
1 2 13
1 2 15
1 3 14
1 3 22
2 1 12
2 1 19
2 1 15
2 1 18
2 2 31
2 3 18
2 3 9
2 3 12



```

data trv ;
infile 'solvar' ;
input sol variete germina ;
run ;
proc glm ;
class sol variete ;
model germina = sol variete sol * variete ;
run ;

```



General Linear Models Procedure
Class Level Information

Class	Levels	Values
SOL	2	1 2
VARIETE	3	1 2 3

Number of observations in data set = 15

General Linear Models Procedure

Dependent Variable : GERMINA

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	5	400.000000	80.000000	6.00	0.0103
Error	9	120.000000	13.333333		
Corrected Total	14	520.000000			

R-Square	C.V.	Root MSE	GERMINA Mean
0.769231	24.34322	3.651484	15.00000

General Linear Models Procedure

Dependent Variable : GERMINA

Source	DF	Type III Sum of Squares	Mean Square	F Value	Pr > F
SOL	1	52.500000	52.500000	3.94	0.0785
VARIETE	2	124.754026	62.377013	4.68	0.0405
SOL*VARIETE	2	222.769574	111.384787	8.35	0.0089

Source	DF	Type III Sum of Squares	Mean Square	F Value	Pr > F
SOL	1	123.7714286	123.7714286	9.28	0.0139
VARIETE	2	192.1276596	96.0638298	7.20	0.0135
SOL*VARIETE	2	222.769574	111.384787	8.35	0.0089

Tableau "Modèle"

General Linear Models Procedure

Class Level Information

Class	Levels	Values
SOL	2	1 2
VARIETE	3	1 2 3

Number of observations in data set = 15

General Linear Models Procedure

Dependent Variable : GERMINA

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	5	400.000000	80.000000	6.00	0.0103
Error	9	120.000000	13.333333		
Corrected Total	14	520.000000			

R-Square	C.V.	Root MSE	GERMINA Mean
0.769231	24.34322	3.651484	15.00000

$$r^2 = \frac{SCE_{M_1} - SCE_{M_3}}{SCE_{M_0}}$$

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	II-1	$SCE_{M_0} - SCE_{M_3}$		$\frac{(SCE_{M_0} - SCE_{M_3}) / II-1}{SCE_{M_1} / N-II}$	
Error	N-II	SCE_{M_1}			
Corrected Total	N-1	SCE_{M_0}			

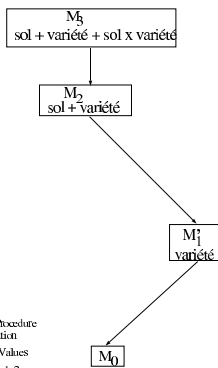
Dependent Variable : GERMINA

Source	DF	Type I SS	Mean Square	F Value	Pr > F
SOL	1	52.5000000	52.5000000	3.94	0.0785
VARIETE	2	124.7340426	62.3670213	4.68	0.0405
SOL*VARIETE	2	222.7659574	111.3829787	8.35	0.0089

Source	DF	Type III SS	Mean Square	F Value	Pr > F
SOL	1	123.7714286	123.7714286	9.28	0.0139
VARIETE	2	192.1276596	96.0638298	7.20	0.0135
SOL*VARIETE	2	222.7659574	111.3829787	8.35	0.0089

Type I			
SOL	I-1	$SCE_{M_0} - SCE_{M_1}$	$\frac{(SCE_{M_0} - SCE_{M_1}) / I-1}{SCE_{M_3} / N-IJ}$
VARIETE	J-1	$SCE_{M_1} - SCE_{M_2}$	$\frac{(SCE_{M_1} - SCE_{M_2}) / J-1}{SCE_{M_3} / N-IJ}$
SOL*VARIETE	IJ-1	$SCE_{M_2} - SCE_{M_3}$	$\frac{(SCE_{M_2} - SCE_{M_3}) / IJ-1}{SCE_{M_3} / N-IJ}$

```
data trv ;
infile 'solvar' ;
input sol variete germina ;
run ;
proc glm ;
class sol variete ;
model germina = variete sol variete*sol ;
run ;
```



General Linear Models Procedure
Class Level Information

Class	Levels	Values
SOL	2	1 2
VARIETE	3	1 2 3

Number of observations in data set = 15

General Linear Models Procedure

Dependent Variable : GERMINA					
Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	5	400.000000	80.000000	6.00	0.0105
Error	9	120.000000	13.333333		
Corrected Total	14	520.000000			
R-Square		C.V.	Root MSE	GERMINA Mean	
0.769231		24.34322	3.651484	15.00000	

General Linear Models Procedure

Dependent Variable : GERMINA					
Source	DF	Type I SS	Mean Square	F Value	Pr > F
VARIETE	2	93.333333	46.666667	3.50	0.0751
SOL	1	83.000792	83.000792	6.29	0.0334
SOL*VARIETE	2	222.7659574	111.3829787	8.35	0.0089
Source	DF	Type III SS	Mean Square	F Value	Pr > F
VARIETE	2	192.1276596	96.0638298	7.20	0.0135
SOL	1	123.7714286	123.7714286	9.28	0.0139
SOL*VARIETE	2	222.7659574	111.3829787	8.35	0.0089

Dependent Variable : GERMINA

Source	DF	Type I SS	Mean Square	F Value	Pr > F
VARIETE	2	93.3333333	46.6666667	3.50	0.0751
SOL	1	83.9007092	83.9007092	6.29	0.0334
SOL*VARIETE	2	222.7659574	111.3829787	8.35	0.0089

Source	DF	Type III SS	Mean Square	F Value	Pr > F
VARIETE	2	192.1276596	96.0638298	7.20	0.0135
SOL	1	123.7714286	123.7714286	9.28	0.0139
SOL*VARIETE	2	222.7659574	111.3829787	8.35	0.0089

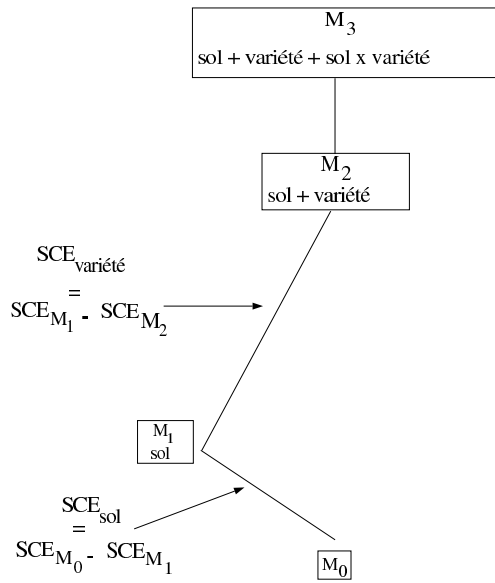
Type I					
VARIETE	J-1	$SCE_{M_0} - SCE_{M_1}$		$\frac{(SCE_{M_0} - SCE_{M_1}) / J-1}{SCE_{M_3} / N-IJ}$	
SOL	I-1	$SCE_{M_1} - SCE_{M_2}$		$\frac{(SCE_{M_1} - SCE_{M_2}) / I-1}{SCE_{M_3} / N-IJ}$	
SOL*VARIETE	IJ-1	$SCE_{M_2} - SCE_{M_3}$		$\frac{(SCE_{M_2} - SCE_{M_3}) / IJ-1}{SCE_{M_3} / N-IJ}$	

Plusieurs sommes de carrés sont disponibles.

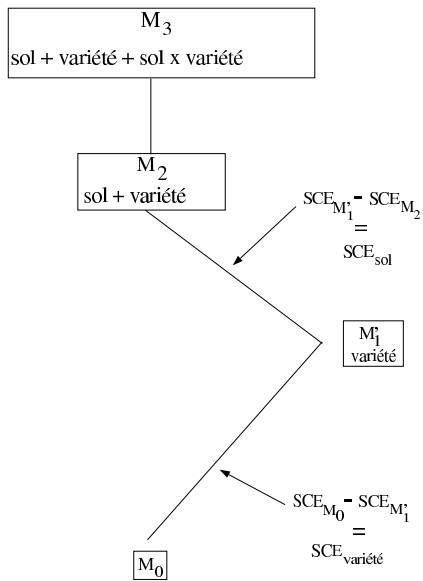
Lesquelles choisir pour tester des modèles ?

Pourquoi ?

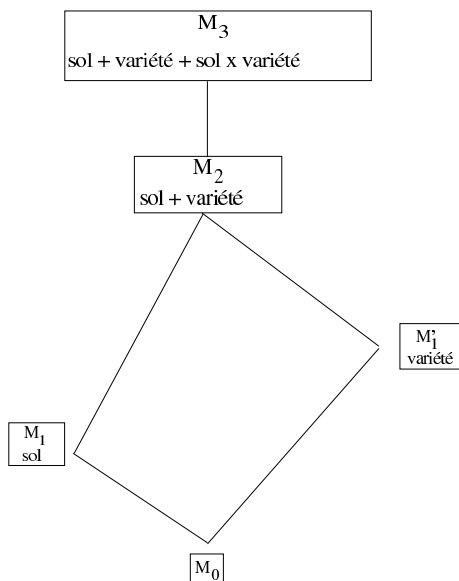
SCE type I :



SCE type I :



SCE type I :



$$SCE_{M_0} - SCE_{M_1'} \neq SCE_{M_1} - SCE_{M_2}$$

$$SCE_{M_0} - SCE_{M_1} \neq SCE_{M_1'} - SCE_{M_2}$$

Illustration géométrique

